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by Meng-choung Chiong

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1 **Moving magnet linear compressor: Operating characteristics under**
2 **resonance and off-resonance frequencies**

4 **ABSTRACT**

5 Objectives: This study compared the accuracy of a Linear Equivalent model and a
6 Fourier Transform model in approximating the resonant frequency of a moving magnet
7 oil-free linear compressor. Furthermore, moving magnet linear compressor
8 performance under resonance and off-resonance frequencies was also examined via an
9 experimental approach.

11 Methods: A Linear Equivalent model and a Fourier Transform model were developed
12 and compared with experimental results at low-pressure ratios of 2-2.5. By varying the
13 operating frequency and compressor piston stroke, the power consumption, compressor
14 losses, efficiency, and cooling capacity are assessed experimentally.

16 Results: This study showed that the disparities between resonance frequencies
17 estimated by theoretical models and experimental data were below 10%. However, the
18 Linear Equivalent model was more accurate than the Fourier Transform model in
19 forecasting the resonance frequency of the linear compressor at a low-pressure ratio of
20 2-2.5. Both experimental and modelling results showed that the resonance frequency of
21 a linear compressor declined with the increasing compressor stroke but increased with
22 increasing pressure ratio. Experiments were also carried out to compare the
23 performance of linear compressors in resonance and off-resonance frequencies. Results
24 showed that the lowest compressor input power of 91.96 W and the highest motor
25 efficiency of 81.98% was achieved when the linear compressor was operated at 38 Hz
26 resonance frequency. Moreover, the cooling capacity has been found to increase by 270
27 W approximately when the linear compressor piston operating stroke extends from 10
28 mm to 13mm.

30 Conclusions: In all, this study showed that the linear compressor motor efficiency is the
31 highest when operating at resonance frequency. However, the cooling capacity of the
32 linear compressor system does not vary significantly with operating frequency. A higher
33 cooling capacity can be achieved by increasing compressor piston stroke.

36 **KEYWORDS:** Linear Equivalent model, Fourier Transform model, Resonance
37 frequency, Cooling capacity, Linear compressor

39 **1. Introduction**

40 As the global economy and human populations continue to grow, the demand for
41 automobiles is also escalating which in turn causes the resulting energy shortage and
42 environmental pollution problems to become more conspicuous (Lü et al., 2018; Shen
43 et al., 2019; Zhang et al., 2021). Speeding up the development of electric vehicles (EVs)
44 can be an effective solution to relieve energy and environmental tensions, it is also a
45 strategic measure to accelerate the transformation of the automobile industry (Ali and
46 Söffker, 2018; Liu et al., 2018; Minh et al., 2021; Qi et al., 2019; Wu et al., 2019). The
47 air conditioning system is one of the major energy-consuming systems of electric
48 vehicles (Essa et al., 2021). The results are confirmatory that air conditioning consumes
49 over 32% traction energy in daily commute, with a significant impact on the all-electric
50 range (Bellocchi et al., 2018). The development of an energy-efficient electric air
51 conditioning system is imminent to foster the adoption of EVs worldwide.

52 Automobile refrigerator compressor can be categorised into the conventional
53 compressor and linear compressors, driven by a rotary motor and linear motor,
54 respectively (Liang, 2018). Conventional compressors use a crank-link mechanism to
55 turn the rotational motion of the rotary motor to a reciprocal linear motion. The
56 drawbacks of cranks usage in mechanical conversion links are high friction losses and
57 high noise levels (Jomde et al., 2018; Sharma and Parey, 2019; Xiao et al., 2019; Zhang
58 et al., 2020). In contrast to conventional compressors, linear compressors eliminate the
59 crank linkage mechanism so that the linear motor drive directly drives the piston in a
60 reciprocating motion. Moreover, at present, nearly all compressors in electric vehicle

61 air conditioning systems utilise a lubrication system. The lubrication system will
62 ⁴¹ increase the structural size and weight of the electric air conditioning system, and the
63 lubricating oil also has adverse effects to the heat exchange efficiency in the condenser
64 and evaporator of air conditioning system (Liang, 2017). As such, it is of great
65 significance to develop an ¹ oil-free linear compressor that can be used in electric vehicle
66 air conditioning systems.

67 A study by Park et al. (2002) highlighted that experimental results showed that
68 linear compressors are 20-30% more efficient than reciprocating compressors using
69 rotary induction motors by comparing the losses of linear and rotary induction motors.
70 The results of an experimental analysis of linear the compressor by Bradshaw showed
71 that it is up to 35% more efficient than a conventional crank-driven reciprocating
72 compressor (Bradshaw et al., 2013). A performance ²⁹ comparison between a moving
73 magnet linear compressor and a reciprocating crank-driven compressor was carried out
74 in an experiment (Liang et al., 2014b). The results showed ⁴³ that linear compressor has a
75 ¹ much higher motor efficiency (86%), while conventional reciprocating compressor
76 showed a lower motor efficiency (60%). The aforementioned studies set out linear
77 compressors present a superior performance as compared to conventional compressors.

78 ² The linear compressor can be modelled as a mass-damper-spring system with
79 optimum operating efficiency is closely related to that of the mass-damper-spring
80 system's frequency (Li et al., 2021). The study of accurate prediction of the optimum
81 operating efficiency is important for achieving efficient compressor operation. Zou et
82 al. (2020) developed a linear compressor dynamic model and showed that the linear

83 compressor system's natural frequency depends on the spring's equivalent stiffness
84 factor, ²⁷ the mass of the moving piston assembly, and the equivalent damping factor of
85 the system. You et al. (2018) have studied the relationship between resonant frequency
86 and linear compressor's intrinsic parameters. It was shown that resonant frequency
87 decreases with increasing moving mass. Xia and Chen (2010) utilised ¹⁹ computational
88 fluid dynamics (CFD) and finite element analysis (FEA) to investigate the frequency of
89 linear compressors, ³⁰ unveiling that the frequency of a moving magnet linear compressor
90 is influenced by mechanical springs and effective gas springs stiffness. Gas springs
91 stiffness is due to the presence of the axial clearance volume at the front of the
92 compressor cylinder. For different types of linear compressors, it is essential to
93 effectively anticipate the gas equivalent spring stiffness values so that the operating
94 frequency can be corrected to its optimum operating conditions.

95 In this paper, a Linear Equivalent model and a Fourier Transform model were
96 employed to estimate the stiffness of a gas spring using ²¹ a moving magnetic oil-free
97 linear compressor (Liang et al., 2016), and the validity of the two models is compared
98 experimentally. The variation in ³⁸ the performance of the linear compressor system under
99 offset resonant operation is also examined. Finally, the effects of variable frequency
100 control and variable stroke control of the linear compressor system on ³⁴ cooling capacity
101 and Coefficient of Performance (COP) are compared.

102 **2. Experimental setup**

103 **2.1 Moving magnet linear compressor**

104 This experiment was carried out on a ¹ moving magnet linear compressor designed
105 by Liang et al. (2016). Different from the other moving magnet linear compressors, its
106 flex spring system consists of two sets of axially separated flex springs, which are
107 mainly used to support the moving piston and limit its displacement along the cylinder
108 axis (Liang et al., 2016). Furthermore, high radial stiffness of flexible spring effectively
109 limits the radial displacement of the piston, prevents wear on the piston and cylinder,
110 and reduces gas residues caused by radial gas leakage (Liang et al., 2016). However,
111 the gas residues are still unavoidable. The residual gas affects equivalent gas stiffness
112 and thus the resonant frequency of the compressor, so it is necessary to model and
113 experimentally study this compressor. Table 1 shows the linear compressor parameters
114 of the designed experiment.

115

116 Table 1. Linear compressor parameters

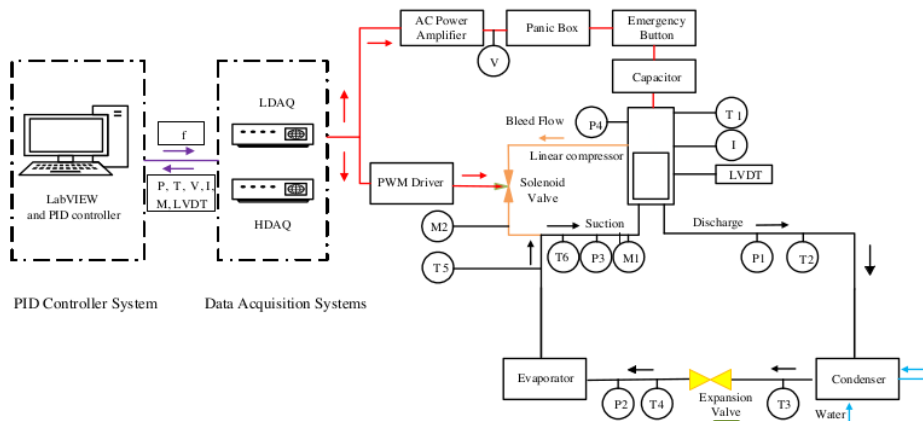
Parameter	Value
Piston mass (kg)	0.66
¹ Coil resistance for each compressor (Ω)	3.5
Distance between the datum position and cylinder head (mm)	7.57
Piston diameter (mm)	18.99
Piston length (mm)	31
Maximum stroke (mm)	14
Clearance between piston and cylinder (mm)	0.0125
Motor force constant (N/A)	30
Damping coefficient (N·s/m)	0.0475
Mechanical Stiffness (N/m)	16284.85

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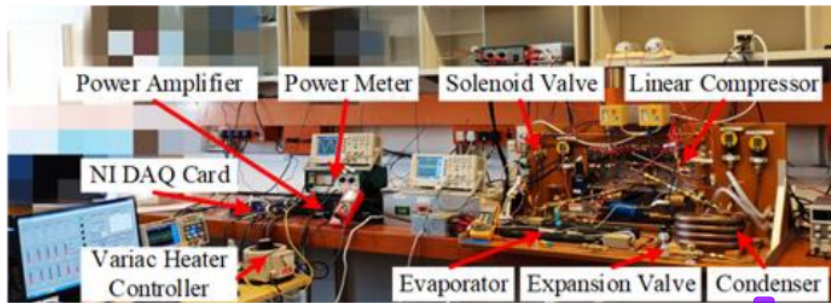
119 **2.2 Test rig**

120 Fig. 1 shows a schematic diagram of the experimental system and Fig. 2 shows the
121 complete test rig. The test rig is equipped with a moving magnet linear compressor, a
122 condenser, an evaporator, four pressure transducers, six thermocouples, two mass flow
123 meters, two current transducers, and two displacement transducers. The pressure
124 transducers are used to measure separately the pressure at the compressor discharge,
125 the evaporator inlet, the compressor suction and the compressor body. The
126 thermocouples are used to measure the temperature in various parts of the system,
127 including compressor body, compressor discharge, condenser outlet, evaporator inlet,
128 evaporator wall, evaporator outlet, and compressor suction. The mass flow meters are
129 used to measure the mass flow in the main and leakage circuits. The current transducers
130 are used to measure the change in current in the two compressor internal coils, and the
131 displacement transducers are used for the measurement of the compressor piston
132 position. The instruments model and accuracy for experimental system can be found in
133 the Table 2.



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135

Fig.1. Schematic diagram of an experimental system (Chen et al., 2019)



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Fig.2. The complete test rig for the moving magnet linear compressor system

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Table 2 List of instruments for the experimental system

Instruments	Model	Accuracy (refer to value)
Pressure transducer	DRUCK PMP1400	±0.15%
Thermocouple	K-type	±1.5°C
Current transducer	LA LEM 25-NP	±0.5%
Voltage attenuator	Fylde 261HVA HV	±0.5%
Mass flow meter	Hastings HFM-201	±1%
LVDT	Lucas Schaevitz	0.025mm

140

2.3 Data Acquisition System

The linear compressor data acquisition system includes a low-speed data acquisition system (LDAQ) and a high-speed data acquisition system (HDAQ). Two NIUSB-6251 data acquisition cards are used in both LDAQ and HDAQ. NIUSB-6251

145 ¹⁶ has 16 analogue inputs (16 bits) and 2 digital outputs with a maximum sampling rate of
 146 1.25MHz for a single channel. The LDAQ is used to collect parameters such as pressure
 147 ⁵ (discharge, suction, compressor body, and evaporator inlet), temperature (discharge,
 148 suction, condenser and evaporator inlet and outlet, compressor body), and mass flow
 149 (main flow and leakage flow); the HDAQ is used to collect data on pressure, voltage,
 150 current and displacement, the HDAQ has a sampling rate of 5000 Hz. More details can
 151 be found in the previous study (Bao et al., 2021).

152

153 2.4 Test Conditions

154 The test condition of this study was set as in Table 3. When the measured pressure
 155 and temperature have reached steady-state and there is no vapor in the condenser and
 156 no liquid in the evaporator, the data acquisition system starts recording and saving the
 157 data.

158

Table 3 The test conditions

Parameter	Value
Working fluid	R134a
Refrigerant charge(g)	309
² Pressure ratio	2.0, 2.5
Stroke(mm)	10-13.5
Condenser outlet temperature (°C)	50
Evaporator inlet temperature (°C)	6-27
Suction temperature (°C)	24-30
Superheat(K)	> 5
Ambient temperature (°C)	20
Compressor body temperature (°C)	> 45

159

160 2.5 Uncertainty analysis

161 ³ Uncertainty analysis is carried out according to the combined uncertainty equations
 162 for two independent uncertainties which can be expressed as:

$$u_{\bar{x}} = \sqrt{s_{\bar{x}}^2 + w_{\bar{x}}^2} \quad (1)$$

163

164 Where $s_{\bar{x}}$ and $w_{\bar{x}}$ are the Type A and B uncertainty.

$$u_{\bar{R}}^2 = \sum_{i=1}^n \left(u_{x_i} \frac{\partial R}{\partial x_i} \right)^2 \quad (2)$$

165

166 Based on Eq. (1) and Eq. (2) (Shen et al., 2022), power consumption, volumetric
167 efficiency, cooling capacity, and COP have a relative uncertainty of 0.95%, 0.24%, 2%,
168 and 2.2%.

169 **2.6. Mathematical model and experimental verification of resonant frequencies**

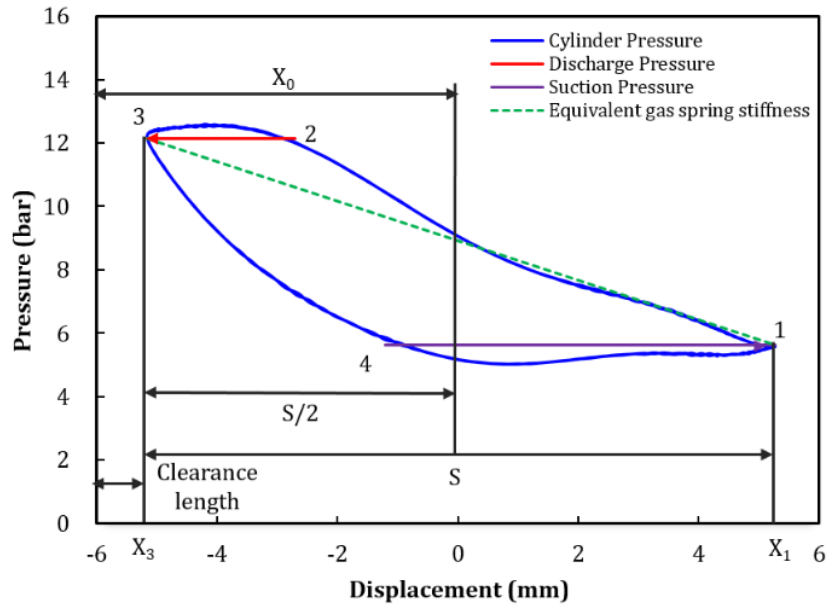
170 **2.6.1 Linear Equivalent model**

171 Linear compressor resonance frequency f_{res} can be expressed using equation (3),
172 where m is moving mass, k_s is mechanical spring stiffness, and k_g is equivalent
173 gas spring stiffness of a linear compressor (Liang, 2018). The presence of a clearance
174 volume at the front end of the compressor cylinder causes residual gas always exists
175 inside the compression chamber during the operation of the compressor. The energy
176 stored in the residual gas is acting as an energy storage spring, and it is therefore
177 modelled as an equivalent gas spring.

178 The value of k_g was estimated based on equation 4, where P_d and P_s are linear
179 compressor discharge and suction pressures, A_p is piston surface area, and S is piston
180 stroke. The slope for equation 4 was acquired based on the slope (green dotted line)
181 between the starting point of the compression stroke (1) and expansion stroke (3) in
182 Fig.3 (Kim et al., 2011).

$$f_{res} = \frac{1}{2\pi} \sqrt{\frac{k_g + k_s}{m}} \quad (3)$$

$$k_g = \frac{P_d - P_s}{S} A_p \quad (4)$$



183

184 Fig.3. Pressure-displacement diagram for linear compressor operated under 38 Hz
 185 frequency, pressure ratio 2.5, and piston stroke 11 mm

186 **2.6.2 Fourier Transform model**

187 The gas equivalent spring stiffness for the Fourier Transform model k_g is given

188 by equation 5(Zou et al., 2014):

$$k_g = -\frac{a_1}{S} \quad (5)$$

189 The a_1 is part of the instantaneous gas force (equation 6) (Tang et al., 2018). The

190 instantaneous gas force is a periodic function that can be expanded into a Fourier series,

191 i.e. the sum of an infinite number of harmonic functions with constant terms. The higher

192 harmonic components of the gas forces have a smaller effect on their amplitude.

193 Therefore, for vibrations at a certain fundamental frequency excitation, it is sufficient

194 to take the first-order harmonic component with the direct current (DC) component.

195 The instantaneous gas force is the sum of an equivalent spring force, a damping force,

196 and an equivalent static force, given by equation 5 (Tang et al., 2018), where a_1 is
 197 related to the equivalent gas spring stiffness (equation 7), b_1 is related to the damping
 198 coefficient, and F_s is related to the piston offset (Li et al., 2022).

$$F_g = a_1 \cos \omega t + b_1 \sin \omega t + F_s \quad (6)$$

$$\begin{aligned} a_1 &= \frac{1}{\pi} \int_0^{2\pi} F_g(t) \cos \omega t d(\omega t) \\ &= \frac{A_p p_s}{\pi} \int_0^{\theta_2} \left(\frac{2X_0 + S}{2X_0 + S \cos \omega t} \right)^n \cos \omega t d(\omega t) + \frac{A_p p_d}{\pi} \int_{\theta_2}^{\pi} \cos \omega t d(\omega t) + \\ &\quad \frac{A_p p_s}{\pi} \int_{\pi}^{\theta_4} \left(\frac{2X_0 + S \cos \theta_4}{2X_0 + S \cos \omega t} \right)^n \cos \omega t d(\omega t) + \frac{A_p p_s}{\pi} \int_{\theta_4}^{2\pi} \cos \omega t d(\omega t) \end{aligned} \quad (7)$$

199 θ_2 and θ_4 are angular positions of the harmonic piston motion at points 2 and 4
 200 respectively in Fig.3, given by equations 8 and 9(KIM, 2000). X_0 is the sum of the
 201 axial clearance length and half of the piston stroke which can be found in Fig.3. $F_g(t)$,
 202 on the other hand, is expressed by equation 10 where $P_c(t)$ is the in-cylinder gas
 203 pressure, P_b is compressor body pressure (Sun et al., 2021).

$$\theta_2 = \cos^{-1} \left[\frac{2X_0}{S} \left(\left(\frac{P_s}{P_d} \right)^{\frac{1}{n}} \left(1 + \frac{S}{2X_0} \right) - 1 \right) \right] \quad (8)$$

$$\theta_4 = \cos^{-1} \left[\frac{2X_0}{S} \left(\left(\frac{P_d}{P_s} \right)^{\frac{1}{n}} \left(1 - \frac{S}{2X_0} \right) - 1 \right) \right] \quad (9)$$

$$F_g(t) = A_p (P_c(t) - P_b) \quad (10)$$

204 To simplify the calculation of gas forces, it was assumed that there are no pressure
 205 fluctuations in the suction and discharge processes. Such assumption was based on a
 206 study showing that pressure fluctuations in the suction and discharge processes have
 207 only insignificant effect on gas forces (Li et al., 2022). The cylinder pressure $P_c(t)$ can
 208 be then expressed as equation 11 (KIM, 2000).

$$P_c(t) = P_r \left(\frac{X_r}{x(t)} \right)^n \quad (11)$$

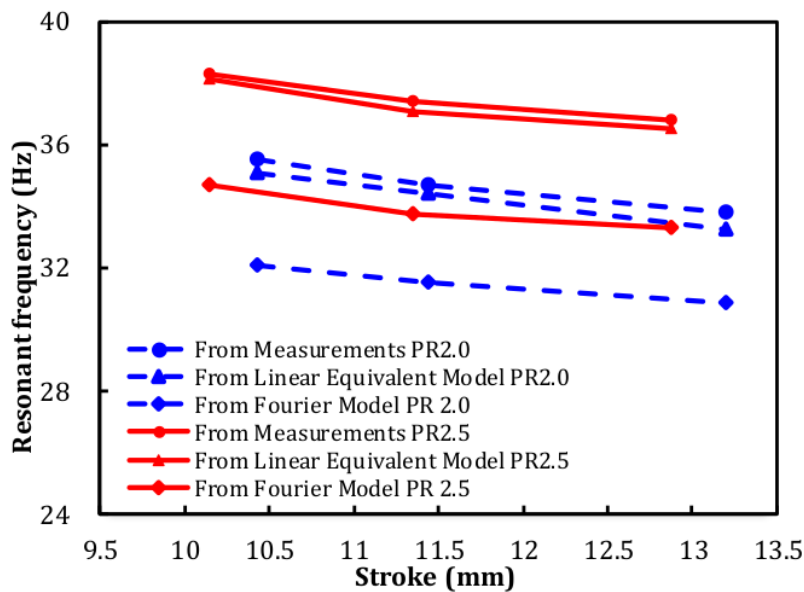
209 Where X_r is ³⁵ reference position, P_r is pressure at that reference position, and n
210 is adiabatic index at 1.13. The reference position is the upper extreme for compression
211 process and the lower extreme for expansion process, which are denoted by X_1 and
212 X_3 respectively ⁸ in Fig.3.

213 **3. Result and discussion**

214 **3.1 Estimation of linear compressor resonant frequency**

215 Fig.4 compares the estimated linear compressor resonant frequency with that
216 obtained experimentally. Compressor pressure ratios 2.0 and 2.5 are considered in this
217 study with compressor stroke varying from 10~13.2 mm. Overall, the resonance
218 frequency of the compressor declines with the increase of compressor operating stroke.
219 Nonetheless, the resonance frequency rises with the elevation of the compressor
220 pressure ratio. Both models exhibit an estimation error of less than 10%, but the Linear
221 Equivalent model is notably more accurate than the Fourier Transform model in
222 approximating the resonant frequency.

223



224

225 Fig.4. Comparison of experimental values and calculated values from two models

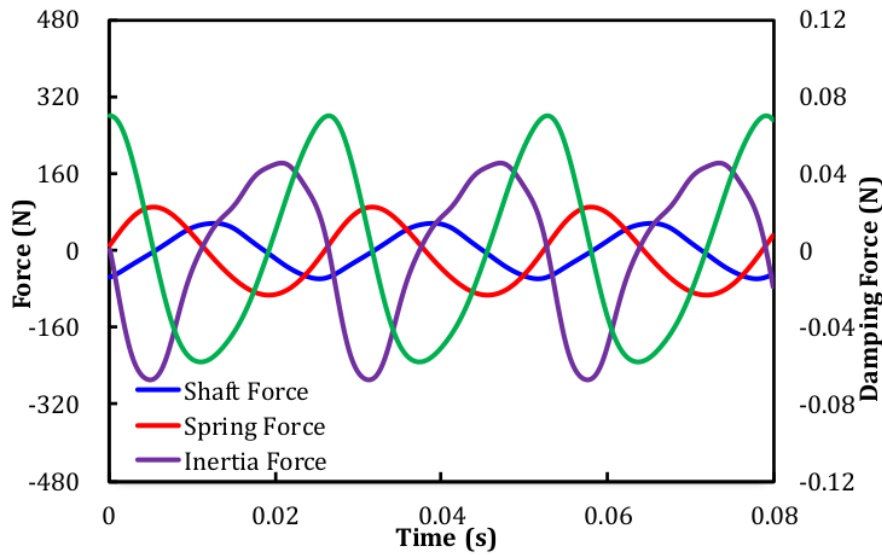
226 The discrepancies between theoretical models and experimental data can be
227 attributed to the existing theoretical models considering only the residual gas due to the

228 clearance volume at the front end of the compressor cylinder and in between ²³piston and
229 cylinder. The presence of a clearance gap between piston and cylinder causes a fraction
230 of the intake gas to be not compressed thus undesirably leading to an energy loss. In
231 practice, however, the residual gas also penetrates the vent and escapes through valves
232 during the gas exchange process (Hwang and Lee, 2019). The gas leaking through
233 valves was not considered in the present model, thus resulting in a less accurate
234 estimation of the equivalent gas spring stiffness and resonant frequency.

235 Furthermore, it can be observed also that the Fourier Transform model exhibits a
236 considerably lower accuracy than the Linear Equivalent model in approximating the
237 compressor resonant frequency. The equivalent gas spring stiffness exhibits highly non-
238 linear characteristics at a high-pressure ratio operation (Liang, 2018), but at the present
239 experimental pressure ratios (2.0 and 2.5) where the non-linear characteristics of the
240 equivalent gas spring are less pronounced, the Linear Equivalent model turns out being
241 a more reliable tool in estimating the equivalent gas spring stiffness and linear
242 compressor resonant frequency. At a higher pressure ratio where non-linear
243 characteristics of the equivalent gas spring are magnified, the Fourier Transform model
244 is expected to give a more accurate estimation of resonant frequency (Bijanazad ¹⁰et al.,
245 2020). The present study shows that the Linear Equivalent model is a more precise tool
246 for estimating the linear compressor resonance frequency at pressure ratios 2.0 and 2.5,
247 a regime where ⁴⁴non-linear characteristics of the equivalent gas spring are less
248 prominent.

249 **3.2 Resonance characteristics of the linear compressor**

250 Fig.5 shows the variation of shaft force, spring force, inertia force and damping
251 force over time for a linear compressor under resonance frequency 38Hz. The shaft
252 force varies continuously with armature, piston position and instantaneous excitation
253 current, so it is difficult to measure the shaft force of the motor directly. The shaft force
254 can be calculated from the Force-Current-Displacement calibration map (Zhu et al.,
255 2021). The shaft force varies sinusoidally over a cycle and peaks at 56.8N at 0.0128s.
256 The spring force is related to the mechanical spring stiffness and piston displacement.
257 The mechanical spring stiffness of the linear compressor is 16284.85 N/m. The real-
258 time displacement in the cylinder can be determined from the piston position measured
259 by a displacement transducer. The piston is closest to the top of the cylinder at 0.0054s.
260 and the mechanical spring force reaches a maximum of 90.1N. The damping force is
261 dependent on the damping coefficient and piston velocity, and the inertia force is
262 determined by the moving mass and piston acceleration. Viscous damping is the most
263 important form of damping for linear compressor pistons. In the calculation of the
264 damping coefficient, the flow in the radial clearance is assumed to be laminar and the
265 radial clearance is a fixed value (Liang et al., 2014a). Linear compressor damping
266 coefficient is about 0.0475 N*s/m and moving mass is 0.66 kg.

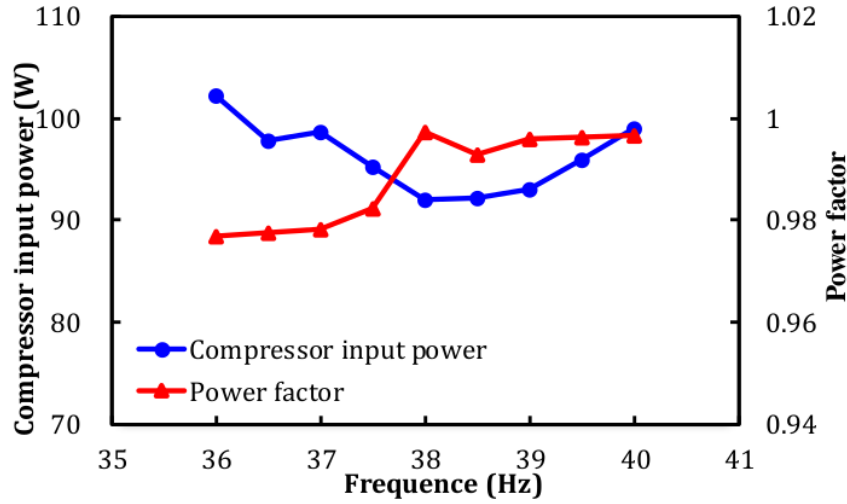


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Fig.5. The variation of shaft force, spring force, inertia force and damping force over time for a linear compressor under resonance frequency

270 3.3. Off-resonance characteristics of the linear compressor

271 Linear compressor off-resonance characteristics were also examined in the range
272 of 36-40 Hz band using a linear compressor with an 11 mm stroke and a 2.5 pressure
273 ratio. Fig.6 illustrates compressor input power and power factor as a function of
274 operating frequency. Compressor power input \dot{W}_{in} was calculated based on the
275 measured voltage and current $\dot{W}_{in} = \frac{1}{t} \int_0^t UI dt$, where U is voltage, I is current, and
276 t is operating period (Sun et al., 2021). The linear motor power factor reflects the
277 utilization ratio of the power input. It can be expressed as $PF = \frac{\dot{W}_{in}}{U_{rms}I_{rms}}$ (Sun et al.,
278 2021). The power input is lowest at operating frequency of 38 Hz (91.96 W), and the
279 power factor is maximum (0.998). As the operating frequency deviates from 38 Hz,
280 power input rises noticeably. The input power rises to 102.3 W at 36 Hz and 99.09 W
281 at 40 Hz.



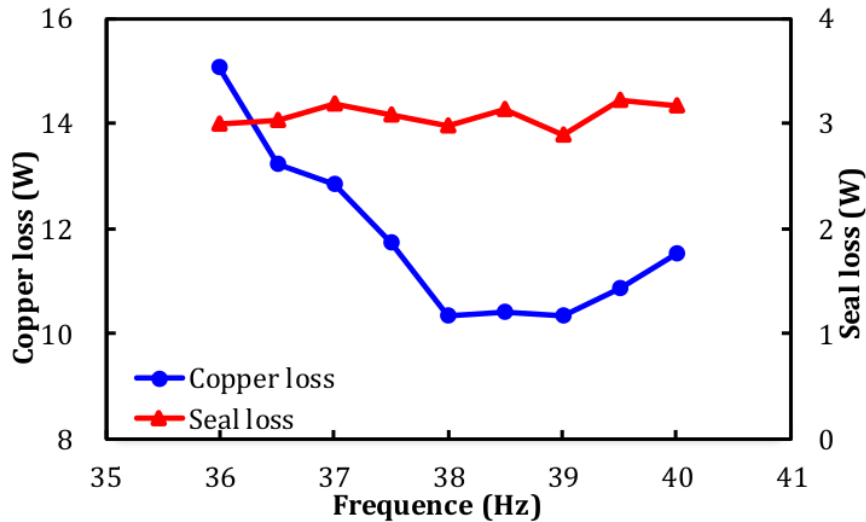
282 Fig.6. Compressor input power and power factor against operating frequency
 283

284 One of the possible reasons that contribute to the lowest input power needed at 38
 285 Hz operating frequency in Fig.6 is the copper and seal losses are found to be minimal
 286 at this specific operating point as demonstrated in Fig.7. The copper loss is the energy
 287 loss due to resistive heating. The copper loss \dot{W}_{copper} was calculated using $\dot{W}_{copper} =$
 288 $I_{rms}^2 R$ (Chen et al., 2020a). Where R is the total coil resistance and I_{rms} is root
 289 mean square (RMS) value of current supplied to the compressor. The seal leakage
 290 power loss \dot{W}_{seal} is expressed by equation 12 (Liang et al., 2013), where c is radial
 291 clearance, μ is viscosity constant, L is clearance length, and P_{1a} is amplitude.

$$\dot{W}_{in} \approx \frac{\pi f D c^3}{24 \mu L} \int \frac{P_{1a}^2 \sin 2\pi f t (2P_b + P_{1a} \sin 2\pi f t)}{P_b + P_{1a} \sin 2\pi f t} \quad (12)$$

292 With reference to Fig.7, the copper loss is minimum at the operating frequency of
 293 38 Hz (~10W). At lower (36 Hz) and higher (40 Hz) operating frequencies, the copper
 294 loss elevates by ~5.1 W and ~2 W, respectively. The seal loss does not vary significantly
 295 with operating frequency, fluctuating at about 3.08 W, as seen in Fig.7. This signifies

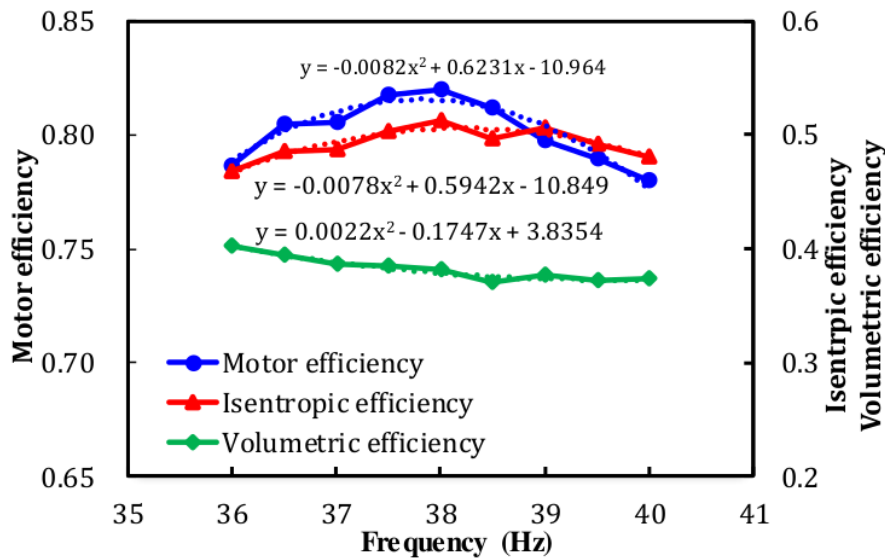
296 that the seal loss is weakly dependent on the operating frequency.



297
298 Fig.7. Copper loss and seal loss against operating frequency

299 Fig.8 shows the motor efficiency and isentropic efficiency against operating
 300 frequency. The motor efficiency η_m and isentropic efficiency η_{isen} can be expressed
 301 as : $\eta_m = \frac{W_{in} - W_{copper}}{W_{in}}$ and $\eta_{isen} = \frac{\dot{m}(h_2 - h_1)}{W_{in}}$ (Sun et al., 2021). Where h_2 is the
 302 isentropic discharge enthalpy of the compressor and h_1 is the suction enthalpy of the
 303 compressor. Owing to the compressor losses being minimum at 38 Hz, the maximum
 304 motor efficiency and isentropic efficiency were acquired at 38 Hz operating frequency,
 305 with a motor efficiency of 81.98 % and an isentropic efficiency of 51.31 %. The motor
 306 efficiency and isentropic efficiency both fell by 3.32 % and 4.47 %, respectively, when
 307 operating at 36 Hz. When the compressor stroke is fixed, volumetric efficiency does
 308 not change considerably with the compressor working frequency. The largest change in
 309 volumetric efficiency while the compressor runs at 36-40 Hz is about 3.2%. As a result,
 310 the compressor that operates at off-resonance consumes approximately 2.8% more

311 energy than that at the resonance frequency.



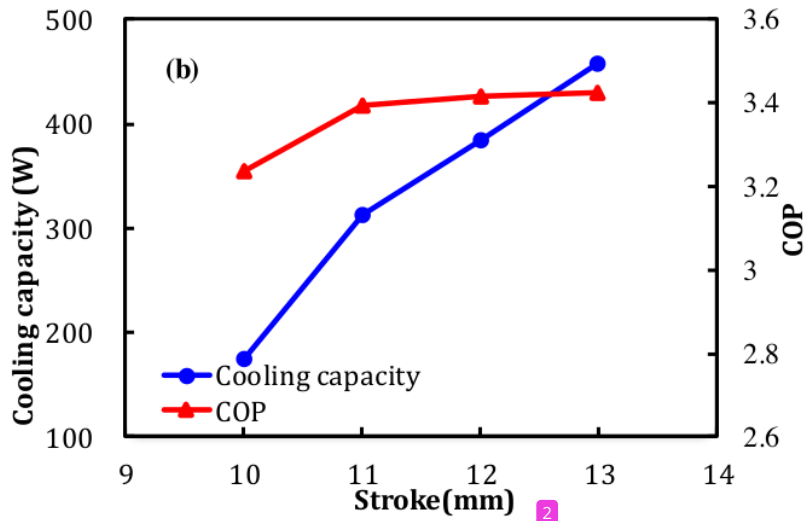
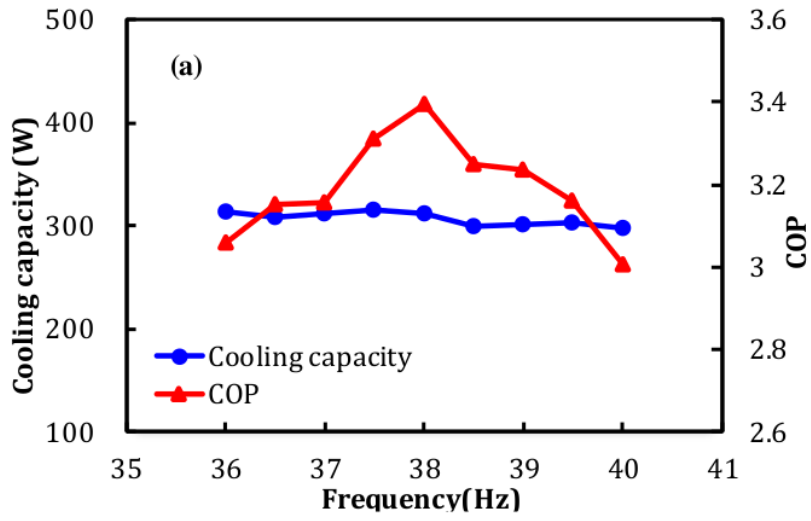
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314 Fig.8. Motor efficiency, isentropic efficiency, and volumetric efficiency against
315 operating frequency

316 Cooling capacity and COP are important indicators for evaluating the performance
317 of refrigeration systems. In contrast to conventional compressors with start-stop
318 regulation and frequency regulation, linear compressors can regulate cooling capacity
319 by varying the drive frequency and piston stroke. Cooling capacity Q_c can be
320 calculated using $Q_c = \dot{m}(h_1 - h_5)$ (Chen et al., 2020b). Where, h_5 is refrigerant
321 enthalpy at compressor inlet. COP was calculated using $COP = \frac{Q_c}{W_{in}}$ (Chen et al.,
322 2020b). Fig.9a shows the COP and cooling capacity at a variable drive frequency for a
323 fixed stroke of 11 mm. The cooling capacity does not change substantially with
324 frequency when the compressor is operating near the resonance frequency. The COP,
325 on the other hand, has a nearly symmetrical tendency over the frequency range. The
326 highest COP is 3.39 and the cooling capacity is 312.17 W when the operating frequency

327 is at the resonance frequency. This is because the input power is low at the resonance
328 frequency. Nonetheless, as the operating frequency is changed from the resonance
329 frequency, the input power increases and the COP declines. The COP reduces to 3.01
330 at 40 Hz.

331 The COP and cooling capacity at the resonant frequency with varying compressor
332 strokes are shown in Fig.9b. With an increasing stroke, cooling capacity and COP rise
333 in a roughly linear fashion. The maximum cooling capacity is 457.96 W and the
334 maximum COP is 3.42 at a stroke of 13 mm. Sun et al. (2021) also found that when
335 piston stroke increases, compressor input power operating at a given frequency with
336 changing strokes also rises. The cooling capacity and input power both increase linearly
337 as the compressor stroke extends, however, the rate of increase in input power is notably
338 lower than the cooling capacity.



339 47
 340 Fig.9. (a) Cooling capacity and COP at a variable drive frequency for a fixed stroke of
 341 11 mm (b) Cooling capacity and COP at a variable stroke for a fixed frequency of 38Hz

342 **4. Conclusion**

343 This study unveils that the linear compressor resonance frequency exhibits a
344 linearly decreasing trend¹ with the increase of compressor operating stroke. Nonetheless,
345 the linear compressor resonance frequency increases significantly (~3 Hz) as the
346 compressor pressure ratio elevates from 2.0 to 2.5. The Linear Equivalent model is more
347 accurate in estimating the compressor resonant frequency than the Fourier Transform
348 model, despite the errors for both models being less than 10% when compared with
349 experimental data. The Linear Equivalent model is evidently a more reliable tool than
350 the Fourier Transform model in approximating linear compressor resonant frequency
351 for pressure ratio 2-2.5.

352 The input power¹¹ required to operate the compressor is the lowest when the
353 compressor is operating at the resonance frequency. The compressor input power
354 increases by a factor of approximately 1.2 as the compressor operating frequency
355 reduces by 2 Hz. Concurrently, the compressor isentropic efficiency reduces by ~3.1%
356 as the compressor operating frequency lowers by 2 Hz. The cooling capacity of a linear⁹
357 compressor system does not vary significantly with the operating frequency; the COP
358 is highest (3.42) at the resonance frequency. The cooling capacity of a linear compressor⁹
359 system can be increased by increasing the compressor operating stroke. The cooling
360 capacity has been found to increase by ~270 W when the compressor operating stroke
361 extends by 3 mm.

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