



# Magnetic anomaly interpretation for a 2D fault-like geologic structures utilizing the global particle swarm method

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## ABSTRACT

We establish a method to interpret the magnetic anomaly due to 2D fault structures, with an evaluation of first moving average residual anomalies utilizing filters of increasing window lengths. After that, the buried fault parameters are estimated using the global particle swarm method. The goodness of fit among the observed and the calculated models is expressed as the root mean squared (RMS) error. The importance of studying and delineating the fault parameters, which include the amplitude factor, the depth to the upper edge, the depth to the lower edge, the fault dip angle, and the position of the origin of the fault, is: (i) solving many problem-related engineering and environmental applications, (ii) describing the accompanying mineralized zones with faults, (iii) describing geological deformation events, (iv) monitoring the subsurface shear zones, (v) defining the environmental effects of the faults before organizing any investments, and (vi) imaging subsurface faults for different scientific studies.

Finally, we show the method applied to two theoretical models including the influence of the regional background and the multi-fault effect and to real field examples from Australia and Turkey. Available geologic and geophysical information corroborates our interpretations.

## 1. Introduction

The magnetic method uses the magnetization contrasts between different lithologies to examine environmental or geologic subsurface problems of various kinds. These problems include subsurface elements and mineral and ore detection (Al-Garni, 2010; Dar and Bukhari, 2020; Mehaneq et al., 2021; Ben et al., 2022a; Saada et al., 2022; Ekwok et al., 2023), hydrocarbon exploration (Osinowo and Taiwo, 2020), archaeological investigation (Essa and Abo-Ezz, 2021), geotechnical engineering (Igwe and Umbugadu, 2020), cave discovery (Orfanos and Apostolopoulos, 2012) and geothermal exploration (Abraham and Alile, 2019). Inversion of magnetic data for arbitrarily complex structure is an ill-posed and non-unique problem (Utsugi, 2019). Interpretation for simple geometric shapes reduces the complexity and offers usable best-fit solutions (Abo-Ezz and Essa, 2016; Essa and Elhussein, 2019; Biswas and Rao, 2021; Ben et al., 2022b).

Graphical and numerical methods have long been used to appraise

simple subsurface geometric-model parameters (Gay, 1963; Abdelrahman et al., 2009; Biswas et al., 2017). Global optimization algorithms have been successfully applied to full complete interpretation (Biswas and Acharya, 2016; Ekinci et al., 2019; Di Maio et al., 2020; Essa, 2021; Essa et al., 2021; Singh and Biswas, 2021; Biswas et al., 2022; Ai et al., 2023).

In this study we present an extended application of the particle swarm method to elucidate the magnetic residual anomaly of 2D fault-like geologic structures. A residual magnetic anomaly is computed using a first moving average to estimate a first-order regional from the observed magnetic anomaly. The proposed method was verified on two theoretical examples. The first example demonstrates the influence of the linear regional field and the second example shows the detection of subsurface multi-faults. The appraised fault parameters ( $K$ ,  $z_1$ ,  $z_2$ ,  $\theta$ ,  $\beta$ , and  $c$  – see Fig. 1) show that the proposed method is firm. After that, the suggested method was applied on two real datasets from Australia and Turkey to obtain the subsurface fault parameters. Finally, the results

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from the examples studied show that the proposed method can tolerate noise and regional background in the observed field and give a good insight into subsurface faults.

## 2. Particle swarm method

The particle swarm optimization is carefully distinguished and has been used to address a variety of geophysical problems. The development of the method was fully described in the published literature (Singh and Biswas, 2016; Essa and Munsch, 2019; Essa, 2021), and we do not repeat it here. Instead, we accentuation on its considerable profits in vanquishing the ill-posedness and non-uniqueness of magnetic data inversion. Furthermore, it is firm, vigorous, and effective in attaining an optimal global solution. The power of the technique is typically seen in the theoretical and field models presented below.

## 3. Forward modelling

For a 2D fault model, the magnetic anomaly (T) at an observation point (P(x<sub>j</sub>)) along a profile (Fig. 1) is given by (e.g., Murthy et al., 2001; Aydin, 2008):

$$T(x_j) = K \left\{ \cos(\theta + \beta) \left[ \operatorname{atan} \left( \frac{(x_j - c) + (z_2 - z_1) \cot \beta}{z_2} \right) - \operatorname{atan} \left( \frac{x_j - c}{z_1} \right) \right] + \left\{ \sin(\theta + \beta) \left[ \ln \left( \frac{\left( ((x_j - c) + (z_2 - z_1) \cot \beta)^2 + z_2^2 \right)^{0.5}}{(x_j - c)^2 + z_1^2} \right) \right] \right\} \right\} \quad (1)$$

where x<sub>j</sub> is the coordinate of the observation station (km), c is the trace point of the fault (km), z<sub>1</sub> is the depth to the upper edge of the fault (km), z<sub>2</sub> is the depth to lower edge (km), β is an inclination angle which include the dip of the effective magnetization and the direction of the measurement (°), θ is the fault dip (°), and K (nT) is the amplitude factor or intensity of magnetization, which depends on the susceptibility contrast (see Fig. 1).

## 4. First moving average method

The total magnetic field anomaly can be decomposed as a residual and a respectively linear regional field, which are related to shallow and deep geologic structures, is:

$$\Delta T_o(x_j) = T(x_j) + \operatorname{Reg}(x_j) \quad (2)$$

where ΔT<sub>o</sub>(x<sub>j</sub>) is the observed magnetic anomaly, T(x<sub>j</sub>) represents the magnetic anomaly due to the 2D fault (residual anomaly) and Reg(x<sub>j</sub>) is the magnetic anomaly due to regional anomaly (deep structures). Removal of the impact of the regional field is considered as one of the most important difficulties in magnetic data elucidation. The first moving average method application is regularly applied for this issue.

Griffin (1949) explained that the first moving average regional is:

$$\operatorname{Reg}(x_j) = \frac{\sum_{j=-n}^{j=+n} \Delta T_o(x_{i+j})}{2n + 1}, \quad n = 1, 2, 3, \dots \quad (3)$$

where the window length operator (s-value) for calculating the moving average regional is equal 2n + 1. Thus, the moving average residual anomaly is:

$$R(x_j, s) = \Delta T_o(x_j) - \frac{\sum_{j=-n}^{j=+n} \Delta T_o(x_{i+j})}{s} \quad (4)$$

The particle swarm optimization method is utilized to the residual (calculated above) to obtain the 2D fault parameters (K, z<sub>1</sub>, z<sub>2</sub>, θ, β, and c).

Finally, the optimum magnetic anomaly fit is reached by seeking the minimum RMS misfit (λ), which is defined as:

$$\lambda = \sqrt{\frac{1}{N} \sum_{i=1}^N [R_j^o(x_j) - R_j^c(x_j)]^2}, \quad (5)$$

where N is the number of measured points, R<sub>j</sub><sup>o</sup> is the observed magnetic anomaly and R<sub>j</sub><sup>c</sup> is the calculated anomaly at the point x<sub>j</sub>. Fig. 2 displays the flow diagram for the proposed method.

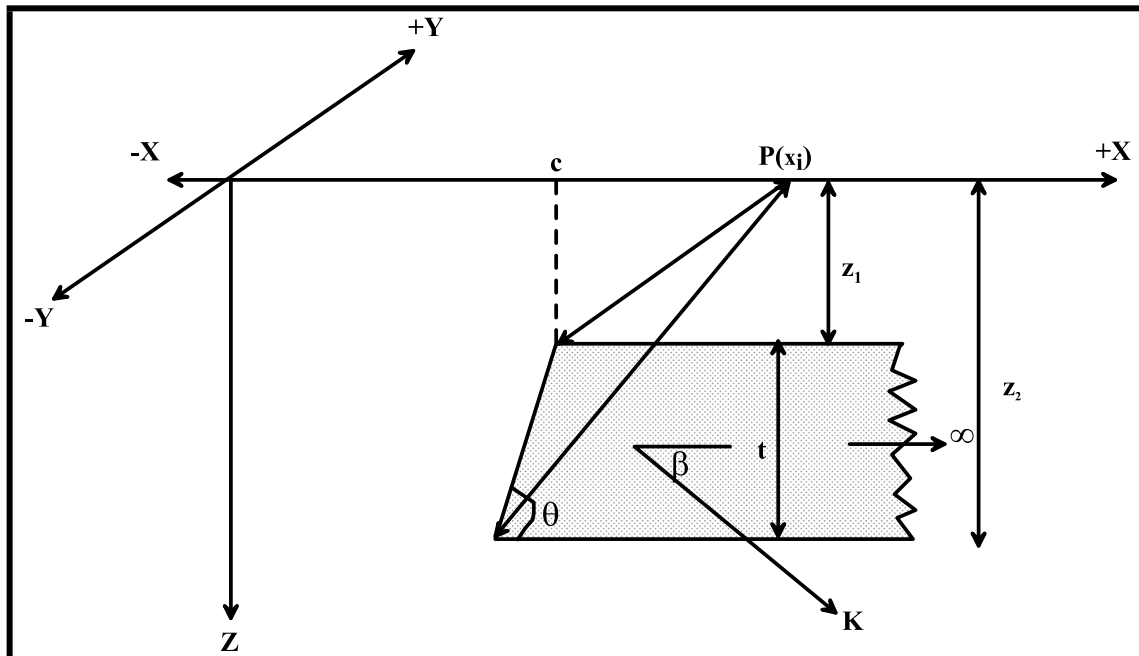


Fig. 1. Sketch diagram for a two-dimensional (2D) fault-like geologic structure and its parameters.

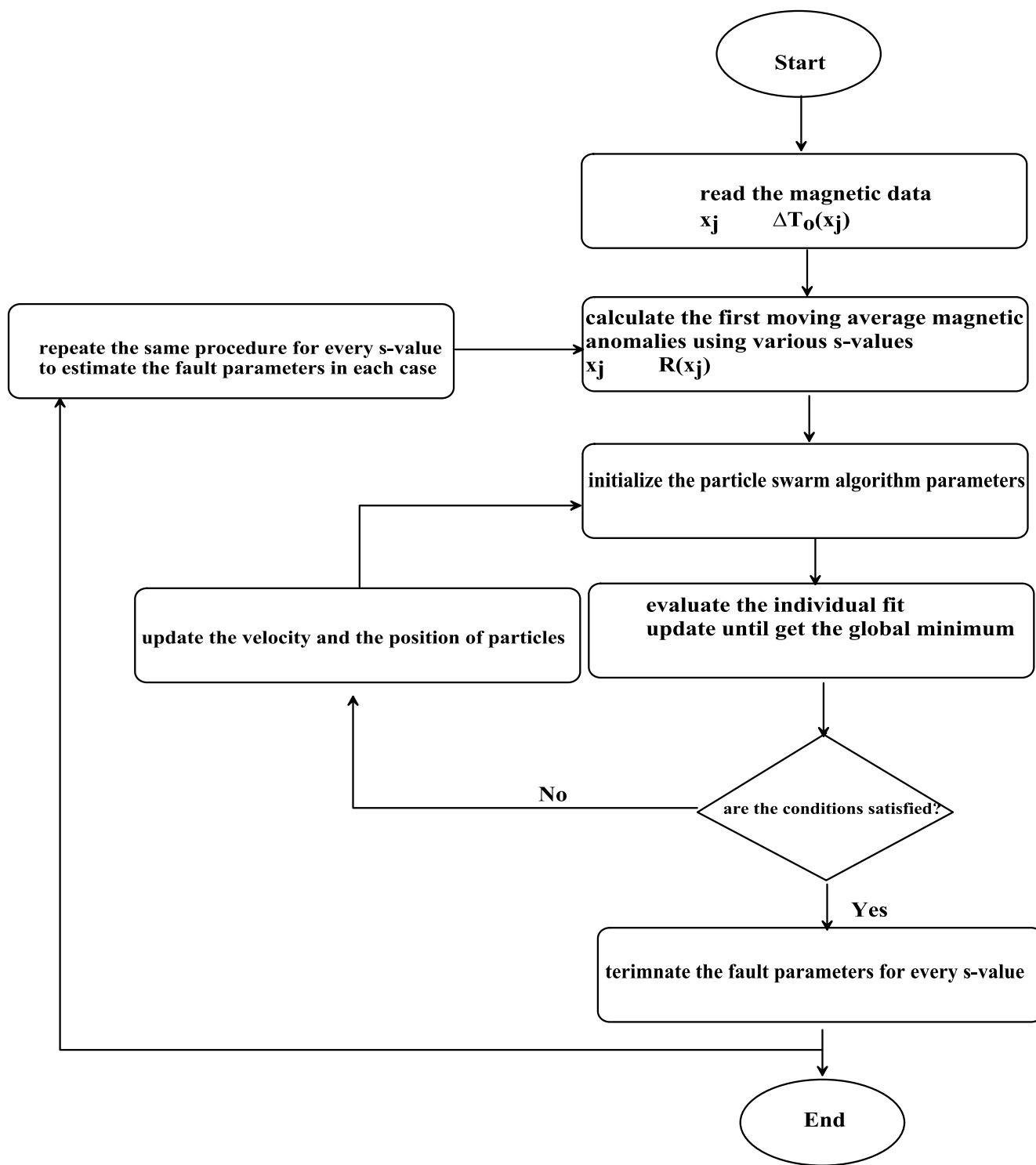


Fig. 2. Flow-chart for the suggested approach.

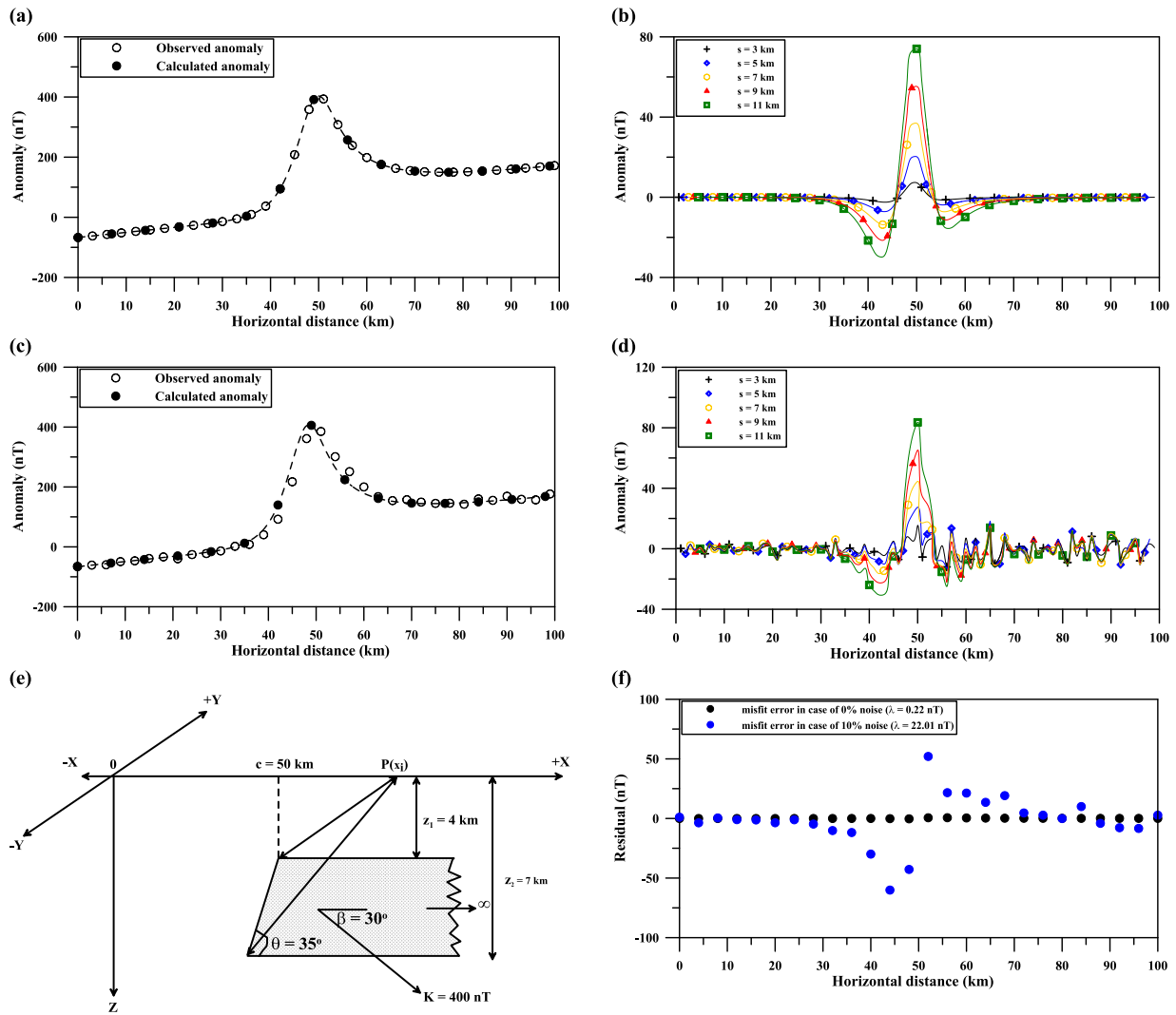
### 5. Theoretical models

We investigated the uncertainties and stability of the suggested technique for assessing the 2D fault model parameters ( $K$ ,  $z_1$ ,  $z_2$ ,  $\theta$ ,  $\beta$ , and  $c$ ) by studying the following two theoretical examples, which revealed the impact of imposed linear regional background and multi-faults effects exemplified by a horst.

#### 5.1. Model 1: Impact of linear regional field

This composite model uses the expected magnetic anomaly ( $\Delta T_o$ ) for the 2D fault described by Equation (1) with the parameters:  $K = 400$  nT,  $z_1 = 4$  km,  $z_2 = 7$  km,  $\theta = 35^\circ$ ,  $\beta = 30^\circ$ ,  $c = 50$  km, and profile length = 100 km and the influence of some unknown deep-structure (regional anomaly) representing by a first-order polynomial ( $2x_j + 50$ ) (Fig. 3a).

We have applied the moving average method to estimate the first moving average residual anomalies by implementing equation (4)



**Fig. 3.** (a) Composite theoretical magnetic anomaly (Model 1). (b) First moving average residual magnetic anomalies for the anomaly in Fig. 3a. (c) Noisy magnetic anomaly. (d) First moving average residual magnetic anomalies for anomaly in Fig. 3c. (e) Geologic sketch of the 2D fault model. (f) Observed and evaluated anomalies misfits in all cases.

**Table 1**

Numerical results due to the application of the global particle swarm method for the first moving average residual magnetic anomalies using several *s*-values for a 2D fault with  $K = 400$  nT,  $K$ ,  $z_1 = 4$  km,  $z_2 = 7$  km,  $\theta = 35^\circ$ ,  $\beta = 30^\circ$ ,  $c = 50$  km, and profile length = 100 km and a first-order impeded regional field anomaly without, with a 10% noise level.

Parameters	Used ranges	Applying the particle swarm method for the first moving average magnetic data							$\mu$	$\delta$ (%)	$\lambda$ (nT)
		with a 0% noise level									
		<i>s</i> = 3 km	<i>s</i> = 5 km	<i>s</i> = 7 km	<i>s</i> = 9 km	<i>s</i> = 11 km					
K (nT)	100–1000	398.23	398.67	399.14	399.50	399.86			$399.08 \pm 0.65$	0.23	0.22
$z_1$ (km)	1–20	3.99	3.99	4.00	3.99	4.00			$3.99 \pm 0.01$	0.15	
$z_2$ (km)	1–20	6.98	6.98	7.00	7.01	6.99			$6.99 \pm 0.01$	0.11	
$\theta$ (°)	10–80	34.96	34.99	34.99	34.99	35.00			$34.99 \pm 0.02$	0.04	
$\beta$ (°)	10–80	29.97	29.99	30.01	30.00	30.00			$29.99 \pm 0.02$	0.02	
<i>c</i> (km)	10–100	49.98	49.98	49.98	50.01	50.01			$49.99 \pm 0.02$	0.02	
with a 10% noise level											
K (nT)	100–1000	382.95	383.13	387.47	389.69	390.24			$386.70 \pm 3.50$	3.33	22.01
$z_1$ (km)	1–20	3.74	3.80	3.84	3.87	3.92			$3.83 \pm 0.07$	4.15	
$z_2$ (km)	1–20	6.71	6.75	6.77	6.81	6.85			$6.78 \pm 0.05$	3.17	
$\theta$ (°)	10–80	32.98	33.36	33.61	34.12	34.38			$33.69 \pm 0.57$	3.74	
$\beta$ (°)	10–80	27.63	28.02	28.14	28.56	29.06			$28.28 \pm 0.55$	5.73	
<i>c</i> (km)	10–100	47.56	47.88	49.15	49.30	49.67			$48.71 \pm 0.93$	2.58	

applying several window lengths ( $s = 3, 5, 7, 9,$  and  $11$  km) (Fig. 3b). Next, the particle swarm was used to gauge the 2D fault parameters ( $K, z_1, z_2, \theta, \beta,$  and  $c$ ) (Table 1). In Table 1, the ranges used for all parameters are presented and the results of the estimated fault parameters are:  $K = 399.08 \pm 0.65$  nT,  $z_1 = 3.99 \pm 0.01$  km,  $z_2 = 6.99 \pm 0.01$  km,  $\theta = 34.99 \pm 0.02^\circ$ ,  $\beta = 29.99 \pm 0.02^\circ$ , and  $c = 49.99 \pm 0.02$  km. The errors in each parameter are vanishingly small and the RMS misfit among the original and the estimated anomalies is 0.22 nT (Fig. 3f). For a noise-free model, this is gratifying but unsurprising.

This method's performance was examined after inserting 10% random noise on the above composite magnetic anomaly (Fig. 3c) applying the next form:

$$\Delta T_o^{\text{rand}}(x_j) = \Delta T_o(x_j) \times [1 + \lambda^*(\text{RAND}(j) - 0.5)], \quad (6)$$

where  $\Delta T_o^{\text{rand}}(x_j)$  is the synthetic model with noise (nT),  $\Delta T_o(x_j)$  is original model (nT),  $\lambda$  is percentage level, and  $\text{RAND}(i)$  is a pseudo-random number whose range is  $[0, 1]$ .

Application of the moving average method with the same window lengths yielded noisy residual magnetic anomalies (Fig. 3d). The global particle swarm optimization gave estimated buried fault structure parameters (Table 1). Table 1 reveals each parameter result as follows:  $K =$

$386.70 \pm 3.50$  nT,  $z_1 = 3.83 \pm 0.07$  km,  $z_2 = 6.78 \pm 0.05$  km,  $\theta = 33.69 \pm 0.57^\circ$ ,  $\beta = 28.28 \pm 0.55^\circ$ , and  $c = 48.71 \pm 0.93$  km, with 3.33%, 4.15%, 3.17%, 3.74%, 5.73%, and 2.58%, respectively. The misfit ( $\lambda = 22.01$  nT) amongst the observed anomaly and the assessed magnetic anomalies is revealed in Fig. 3f.

The results for 0% and 10% noise level imposed on the composite magnetic anomaly reveals the suggested method was capable to cope with the regional background and noise and created valid results.

### 5.2. Model 2: Multi-fault consisting of a horst

We examined a 100 km composite magnetic profile due to multi-fault structures consisting of a horst block with the following parameters:  $K_1 = 300$  nT,  $z_{11} = 3$  km,  $z_{21} = 10$  km,  $\theta_1 = 120^\circ$ ,  $\beta_1 = 20^\circ$ , and  $c_1 = 53$  km for body 1 and  $K_2 = 200$  nT,  $z_{12} = 5$  km,  $z_{22} = 10$  km,  $\theta_2 = 135^\circ$ ,  $\beta_2 = 20^\circ$ , and  $c_2 = 47$  km for body 2 along 100 km profile (Fig. 4a and 4e).

The first moving average method was employed to the magnetic anomaly exploiting several  $s$ -values ( $s = 3, 5, 7, 9,$  and  $11$  km) (Fig. 4b); subsequent the particle swarm method was claimed in order to assess the subsurface faults structures parameters (Table 2). Table 2 indicates the outcomes for the two fault structures, which consist of a horst block, which are:  $K_1 = 290.56 \pm 3.96$  nT,  $z_{11} = 2.93 \pm 0.02$  km,  $z_{21} = 10.00 \pm$

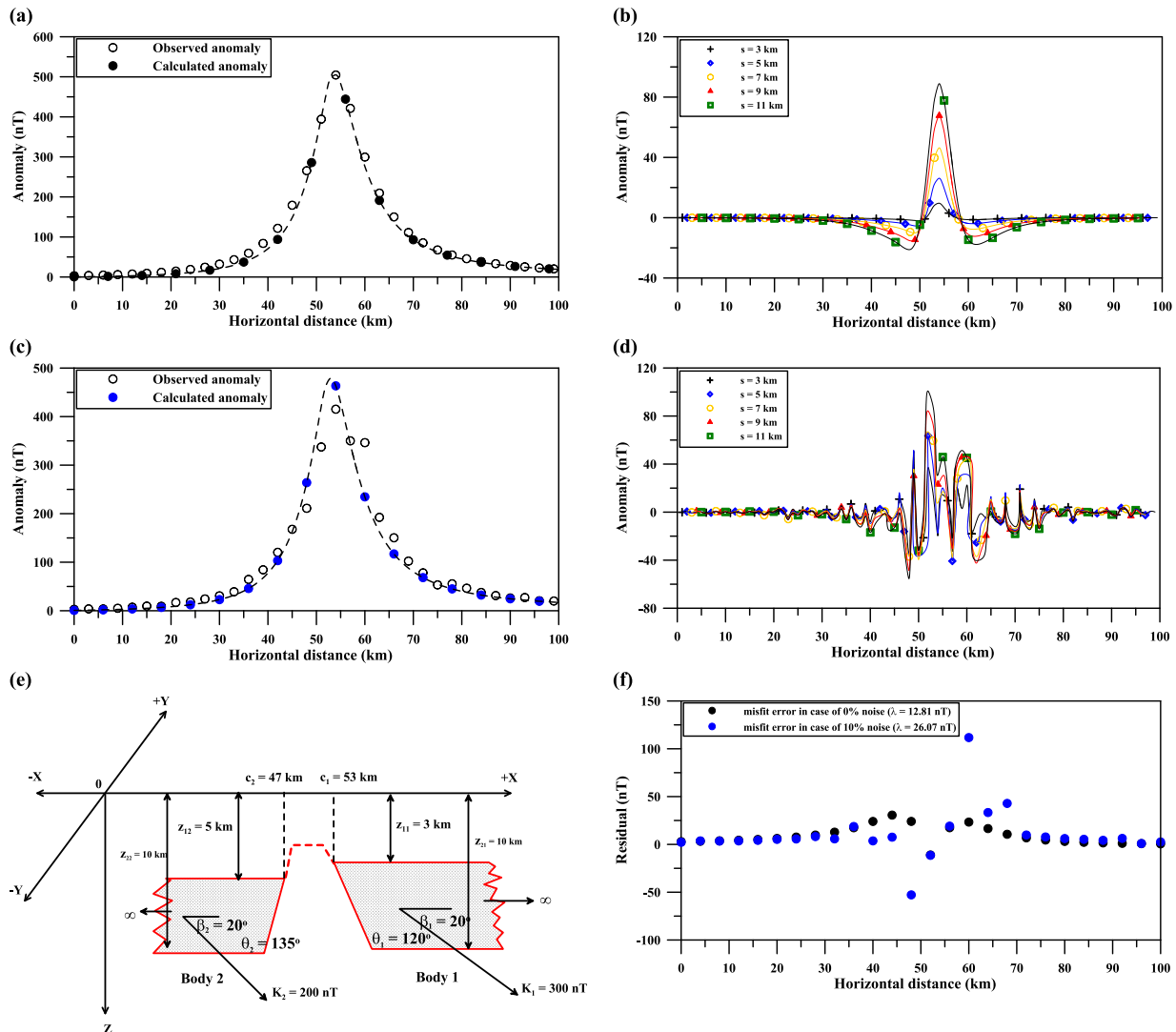


Fig. 4. Composite theoretical magnetic anomaly (Model 2). (b) First moving average residual magnetic anomalies for anomaly in Fig. 4a. (c) Noisy magnetic anomaly. (d) First moving average residual magnetic anomalies for the anomaly in Fig. 4c. (e) 2D fault sketch. (f) Observed and evaluated magnetic anomalies misfits in all cases.

**Table 2**

Numerical results due to the application of the global particle swarm method for the first moving average residual magnetic anomalies using several s-values for the multi-2D faults without and with a 10% noise level.

Model	Parameters	Used ranges	Applying the particle swarm method for the first moving average magnetic data							
			with a 0% noise level							
			s = 3 km	s = 5 km	s = 7 km	s = 9 km	s = 11 km	$\mu$	$\delta$ (%)	$\lambda$ (nT)
Body1	K (nT)	100–500	285.13	288.10	291.32	293.27	294.96	290.56 ± 3.96	3.15	12.81
	$z_1$ (km)	1–20	2.91	2.91	2.95	2.93	2.95	2.93 ± 0.02	2.33	
	$z_2$ (km)	1–20	9.84	9.87	9.92	9.93	9.96	10.00 ± 0.05	0	
	$\theta$ (°)	10–170	117.11	117.64	118.14	119.02	119.00	118.18 ± 0.84	1.52	
	$\beta$ (°)	10–80	18.81	19.19	19.50	19.85	19.93	19.46 ± 0.47	2.72	
	c (km)	10–100	52.05	52.48	52.66	52.84	52.94	52.59 ± 0.35	0.77	
Body2	K (nT)	100–500	192.09	194.26	195.72	196.90	196.88	195.17 ± 2.03	2.41	
	$z_1$ (km)	1–20	4.58	4.70	4.76	4.92	4.92	4.78 ± 0.15	4.48	
	$z_2$ (km)	1–20	8.23	8.68	8.94	9.23	9.54	8.92 ± 0.50	10.76	
	$\theta$ (°)	10–170	129.44	132.31	136.00	136.05	136.38	134.04 ± 3.06	0.71	
	$\beta$ (°)	10–80	18.06	18.42	19.02	19.54	19.80	18.97 ± 0.73	5.16	
	c (km)	10–100	45.33	45.94	46.28	46.61	46.94	46.22 ± 0.62	1.66	
with a 10% noise level										
Body1	K (nT)	100–500	271.24	276.76	283.81	285.25	293.59	282.13 ± 8.53	5.96	26.07
	$z_1$ (km)	1–20	2.82	2.86	2.90	3.01	2.97	2.91 ± 0.08	2.93	
	$z_2$ (km)	1–20	8.75	9.10	10.12	9.91	9.93	9.56 ± 0.60	4.38	
	$\theta$ (°)	10–170	114.36	116.71	118.25	121.48	123.81	118.92 ± 3.76	0.90	
	$\beta$ (°)	10–80	18.19	20.03	19.86	20.57	21.14	19.96 ± 1.11	0.21	
	c (km)	10–100	50.48	51.05	51.74	52.60	53.25	51.82 ± 1.12	2.22	
Body2	K (nT)	100–500	185.03	188.17	193.44	199.00	204.13	193.95 ± 7.78	3.02	
	$z_1$ (km)	1–20	4.41	4.74	4.92	5.13	5.20	4.88 ± 0.32	2.40	
	$z_2$ (km)	1–20	8.15	8.49	9.26	9.74	10.04	9.14 ± 0.80	8.64	
	$\theta$ (°)	10–170	130.36	132.06	133.57	134.61	134.85	133.09 ± 1.88	1.41	
	$\beta$ (°)	10–80	17.47	18.11	18.85	18.92	19.53	18.58 ± 0.80	7.12	
	c (km)	10–100	46.22	47.23	47.62	47.85	47.85	47.35 ± 0.68	0.75	

0.05 km,  $\theta_1 = 118.18 \pm 0.84^\circ$ ,  $\beta_1 = 19.46 \pm 0.47^\circ$ , and  $c_1 = 52.59 \pm 0.35$  km, and the error of  $K_1$ ,  $z_{11}$ ,  $z_{21}$ ,  $\theta_1$ ,  $\beta_1$ , and  $c_1$  are: 3.15%, 2.33%, 0%, 1.52%, 2.72%, and 0.77%, respectively, while the calculated parameters of the second model (Body 2; Fig. 4e) are:  $K_2 = 195.17 \pm 2.031$  nT,  $z_{12} = 4.78 \pm 0.15$  km,  $z_{22} = 8.92 \pm 0.50$  km,  $\theta_2 = 134.04 \pm 3.06^\circ$ ,  $\beta_2 = 18.97 \pm 0.73^\circ$ , and  $c_2 = 46.22 \pm 0.62$  km, and the error of  $K_2$ ,  $z_{12}$ ,  $z_{22}$ ,  $\theta_2$ ,  $\beta_2$ , and  $c_2$  are: 2.41%, 4.48%, 10.76%, 0.71%, 5.16%, and 1.66%, correspondingly, and the RMS misfit ( $\lambda$ -value) is 12.81 nT.

We then imposed a 10% random error on the anomaly (Fig. 4c) using the previous (Eq. (6)). The first moving average residual magnetic anomalies were calculated using the same s-values as before (Fig. 4d), and the fault parameters estimated via the global particle swarm method (Table 2). As shown in Table 2, the predicated parameters of the first model (Body 1; Fig. 4e) are:  $K_1 = 282.13 \pm 8.53$  nT,  $z_{11} = 2.91 \pm 0.08$  km,  $z_{21} = 9.56 \pm 0.60$  km,  $\theta_1 = 118.92 \pm 3.76^\circ$ ,  $\beta_1 = 19.96 \pm 111^\circ$ , and  $c_1 = 51.82 \pm 1.12$  km, and the errors in  $K_1$ ,  $z_{11}$ ,  $z_{21}$ ,  $\theta_1$ ,  $\beta_1$ , and  $c_1$  are: 5.96%, 2.93%, 4.38%, 0.90%, 0.21%, and 2.22%, respectively, while the estimated parameters of the second model (Body 2; Fig. 4e) are:  $K_2 = 193.95 \pm 7.78$  nT,  $z_{12} = 4.88 \pm 0.32$  km,  $z_{22} = 9.14 \pm 0.80$  km,  $\theta_2 = 133.09 \pm 1.88^\circ$ ,  $\beta_2 = 18.58 \pm 0.80^\circ$ , and  $c_2 = 47.35 \pm 0.68$  km, and the error of  $K_2$ ,  $z_{12}$ ,  $z_{22}$ ,  $\theta_2$ ,  $\beta_2$ , and  $c_2$  are: 3.02%, 2.40%, 8.64%, 1.41%, 7.12%, and 0.75%, correspondingly, with an RMS misfit of 26.07 nT.

The misfit amongst the original anomaly and the calculated anomaly (Fig. 4a and Fig. 4c) is shown in Fig. 4f.

In summary, the particle swarm method has been employed on two theoretical models, which represent the effect of a linear regional background and noise (Model 1), and the effect of multi-faults (Model 2). A respectable match of the observed to the calculated model parameters has been found and the errors in all assessed parameters do not increase more than 10%.

## 6. Real data examples

To inspect the practical applicability of the proposed method, two real data sets were collected from the available published literature from Australia and Turkey. The particle swarm method was used to invert the

observed magnetic field values to achieve the optimum fit of the fault parameters ( $K$ ,  $z_1$ ,  $z_2$ ,  $\theta$ ,  $\beta$ , and  $c$ ), which were then compared with current geologic information and any additional geophysical outcomes.

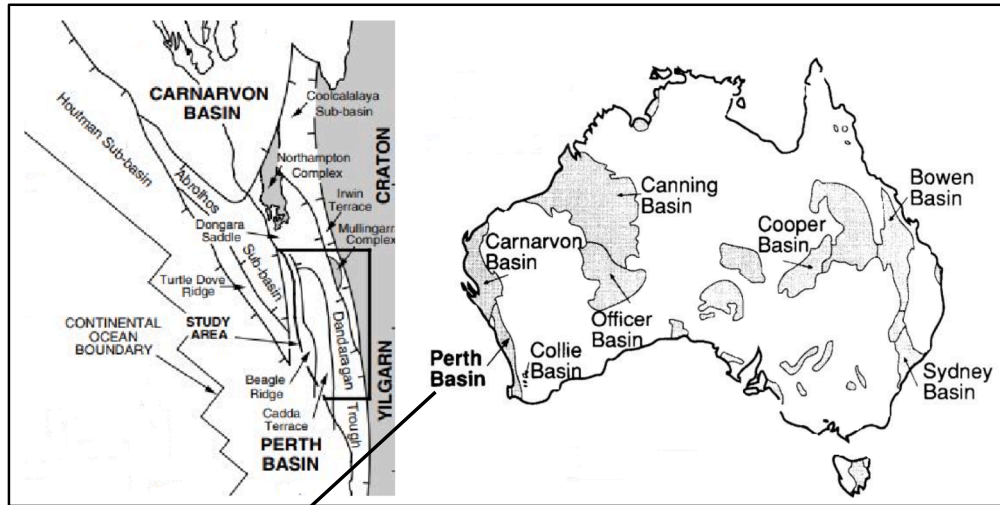
### 6.1. The Perth basin field example, Australia

The Perth Basin is placed at the western part of Australia and is elongated north-to-south. It is effectively the southern part of the Carnarvon Basin and covers an area of about 100,000 km<sup>2</sup>. It is considered as an important basin for hydrocarbon exploration in Australia and includes more than twenty commercial oil and gas fields. The Perth Basin is a huge rift structure, which formed during intra-continental rifting and developed through eventual division of India from Australia. This basin is separated to fifteen sub-basins, which record a big sedimentary fill ranging from Permian to Recent age (Harris, 1994; Olierook et al., 2015) (Fig. 5a).

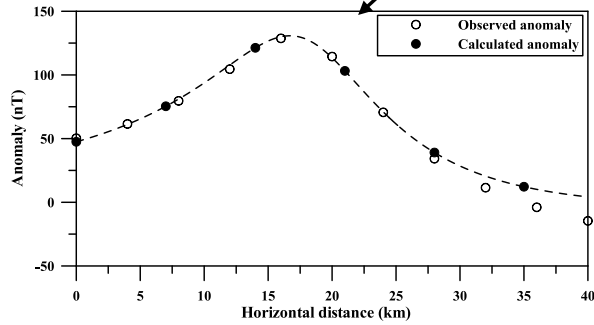
The observed magnetic anomaly owing to a fault-like geologic structure was collected at the Western border of the Perth basin, Australia (Qureshi and Nalaye 1978). The profile length of 40 km was digitized at 1 km intervals (Fig. 5b). This digitized anomaly was used to gauge the parameters  $K$ ,  $z_1$ ,  $z_2$ ,  $\theta$ ,  $\beta$ , and  $c$  using the proposed method for available first moving average residual magnetic anomalies (Fig. 5c) using  $s = 3, 5, 7, 9$ , and 11 km (Table 3). Table 3 demonstrates the extents and results of the fault model parameters as follows:  $K = 146.62 \pm 1.04$  nT,  $z_1 = 5.98 \pm 0.26$  km,  $z_2 = 14.99 \pm 0.35$  km,  $\theta = 95.64 \pm 0.29^\circ$ ,  $\beta = -21.14 \pm 1.92^\circ$ , and  $c = 18.05 \pm 0.42$  km. The misfit (RMS value,  $\lambda = 7.18$  nT) of the original anomaly and the predicated magnetic anomalies is given in profile in Fig. 5e.

The estimated fault parameters by the application of the global particle swarm convolved with the first moving average have a respectable agreement with the results achieved from borehole information (Qureshi and Nalaye 1978);  $z_1 = 5.80$  to 6.85 km,  $z_2 = 15.55$  to 17 km,  $\theta = 30^\circ$  and additional interpretation methods, for example; Rao and Babu (1983) estimated the parameters as follows:  $z_1 = 6.26$  km,  $z_2 = 15.45$  km,  $\theta = 40^\circ$ . Tlas and Asfahani (2011) calculated the parameters  $K = 200.56$  nT,  $z_1 = 7.22$  km,  $z_2 = 13.72$  km,  $\theta = 35.56^\circ$ . Di Maio

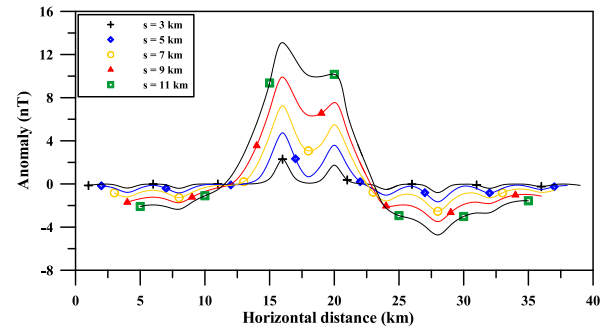
(a)



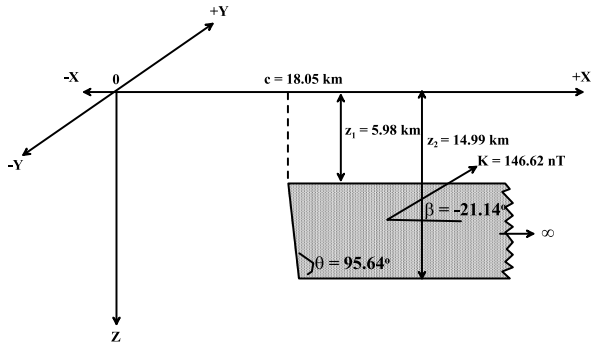
(b)



(c)



(d)



(e)

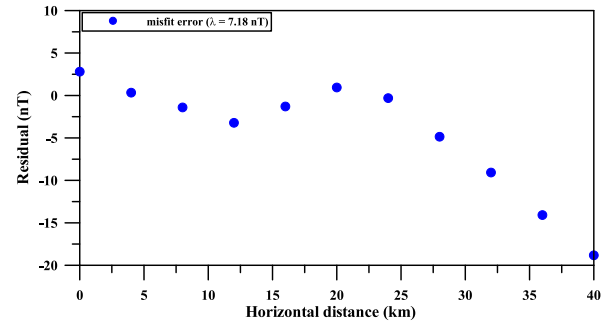


Fig. 5. (a) Location and geologic map of the Perth Basin, Western Australia (after Mory and Iasky, 1996). (b) Observed and calculated magnetic anomalies for the Perth Basin field example, Australia. (c) First moving average residual magnetic anomalies for the anomaly in Fig. 5b. (d) Geologic model of the evaluated 2D fault. (e) Observed and evaluated magnetic anomalies misfit.

Table 3

Numerical results due to the application of the global particle swarm method for the first moving average residual magnetic anomalies using several s-values for the Perth Basin field example, Australia.

Parameters	Used ranges	Applying the particle swarm method for the first moving average magnetic data						$\mu$	$\lambda$ (nT)
		s = 3 km	s = 5 km	s = 7 km	s = 9 km	s = 11 km			
K (nT)	50–500	145.19	146.03	146.72	147.34	147.80	$146.62 \pm 1.04$	7.18	
$z_1$ (km)	1–20	5.65	5.87	5.93	6.12	6.34	$5.98 \pm 0.26$		
$z_2$ (km)	1–20	14.58	14.76	14.98	15.17	15.48	$14.99 \pm 0.35$		
$\theta$ (°)	10–170	95.27	95.68	95.42	95.91	95.91	$95.64 \pm 0.29$		
$\beta$ (°)	–80+80	–18.84	–19.59	–21.35	–22.48	–23.43	$–21.14 \pm 1.92$		
c (km)	5–40	17.41	17.90	18.24	18.53	18.17	$18.05 \pm 0.42$		

et al. (2020) interpreted the fault parameters as follows:  $K = 169.40$  nT,  $z_1 = 8.50$  km,  $z_2 = 12$  km,  $\theta = 35.86^\circ$ . In more detail, the previous inversion methods used the observed magnetic anomaly as a residual anomaly, with no attempt to remove a regional, which is not clear in the respective papers.

6.2. The Şereflikoçhisar-Aksaray fault field example, Turkey

The city of Aksaray is situated in the southwest of the central part of Anatolia between the Sakarya Region and Pontides (Eurasian Plate) in the north and the Anatolide-Tauride Platform in the south. The area is surrounded by young sediments consisting of tertiary units and surrounded by massive metamorphic rocks, comprised of mica schists, graphite schists, phyllites quartzites and marbles. Also, a granitoid intrusion is found in the eastern part of the Şereflikoçhisar-Aksaray fault

and Cappadocian volcanic rocks occasioned from tectonic activities due to the subduction of the Neo-Tethys Ocean. (Aydemir and Ates, 2006; Bilim et al., 2015) (Fig. 6a).

The magnetic anomaly profile for the Aksaray fault, Turkey (Aydemir and Ates, 2006; Fig. 6) with a length of 25 km and digitized at an interim of 0.625 km (Fig. 6b) was employed. A complete interpretation of this magnetic anomaly was done by applying the same procedure as above. The first moving average residual magnetic anomalies were achieved for numerous window lengths ( $s = 1.875, 3.125, 4.375, 5.625,$  and  $6.875$  km) (Fig. 6c). The particle swarm method was employed to these anomalies to evaluate the fault parameters (Table 4). The results in Table 4 are:  $K = 146.07 \pm 1.38$  nT,  $z_1 = 1.95 \pm 0.07$  km,  $z_2 = 4.60 \pm 0.15$  km,  $\theta = 163.29 \pm 0.98^\circ$ ,  $\beta = 33.48 \pm 0.49^\circ$ , and  $c = 540.53 \pm 2.83$  km. As well, the misfit (RMS value  $\lambda = 25.93$  nT) among the observed and the estimated magnetic anomalies is depicted in Fig. 6e.

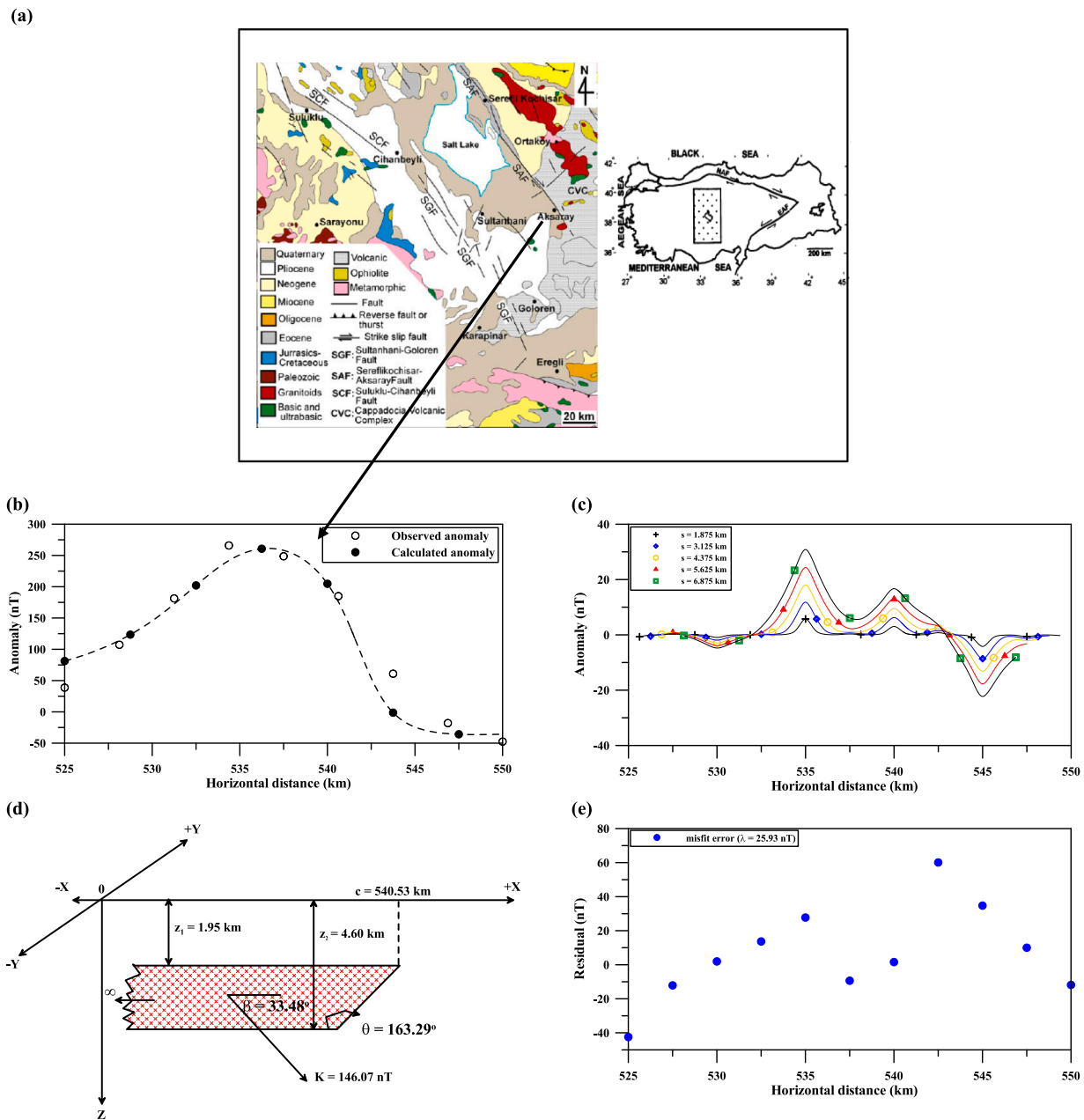


Fig. 6. (a) Location and geologic map of the Şereflikoçhisar-Aksaray fault field example, Turkey (after Bilim et al., 2015). (b) Observed and the calculated magnetic anomalies for the Aksaray fault field example, Turkey. (c) First moving average residual magnetic anomalies for the anomaly in Fig. 6b. (d) Geologic model of the buried 2D fault. (e) Observed and calculated anomalies misfit.



**Table 4**

Numerical results due to the application of the global particle swarm method for the first moving average residual magnetic anomalies using several s-values for the Aksaray fault field example, Turkey.

Parameters	Used ranges	Applying the particle swarm method for the first moving average magnetic data					$\mu$	$\lambda$ (nT)
		s = 1.875 km	s = 3.125 km	s = 4.375 km	s = 5.625 km	s = 6.875 km		
K (nT)	50–500	144.14	145.35	147.72	146.28	146.84	146.07 ± 1.38	25.93
$z_1$ (km)	1–20	1.86	1.91	1.95	2.04	1.98	1.95 ± 0.07	
$z_2$ (km)	1–20	4.53	4.46	4.51	4.67	4.83	4.60 ± 0.15	
$\theta$ (°)	10–170	162.09	162.67	163.10	164.15	164.42	163.29 ± 0.98	
$\beta$ (°)	5–80	32.96	33.08	33.42	33.83	34.11	33.48 ± 0.49	
c (km)	525–550	536.18	539.21	541.83	542.34	543.08	540.53 ± 2.83	

Lastly, the fault model parameters estimated by the proposed method show good agreement with published values, especially the depths to the top and bottom, from Aydemir and Ates (2006) ( $z_1 = 1.92$  km and  $z_2 = 4.61$  km).

## 7. Conclusions

The application of the particle swarm method for interpreting the first moving average residual magnetic anomalies, which is produced from the observed magnetic anomaly using several window lengths, is likely to be useful in geophysical exploration, including hydrocarbon, mineral and ore exploration because it offers several benefits, namely: (1) it removes the effect of deep structures (regional background response), (2) it eliminates the effect of neighbouring structures and noise response, (3) it infers the fault model parameters with a good accuracy, and (4) the method is automatic. The accuracy and pertinence of the proposed method were verified by examining two appropriate theoretical models and two real data sets from Australia and Turkey. From results demonstrate that, the proposed method is robust and stable. This method can be extended to more complicated cases, which we propose to do in a future study.

## Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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